

1 **HERITAGE PRESERVATION BY COMBINING RADIOMETRIC AND GEOMETRIC**
2 **ANALYSIS OF TLS DATA: THE SAN FRANCISCO MASTER GATE IN ALMEIDA**
3 **(PORTUGAL)**

4
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17
18 **Abstract**

19
20 Damage mapping is considered a critical stage in the correct diagnosis of the state of conservation
21 of Cultural Heritage manifestations. The common approach generally implies a large user
22 interaction to map the different pathological processes presented on 2D documents such as
23 elevations or sections, among others. In contrast with this practice, the present paper proposes a
24 semiautomatic 3D-methodology, with a minimum user interaction, able to accurately analyse both
25 radiometric and geometric data recovered by a non-contact technology (Terrestrial Laser
26 Scanning), allowing the extraction and quantification of a wide diversity of pathological processes
27 from biological colonization to deformations. This approach is therefore a potential tool for the
28 rapid and accurate diagnosis of Cultural Heritage. To confirm the applicability and potential
29 offered by the proposed methodology, a highly affected historical masonry, the San Francisco
30 Master Gate of the Almeida Fortress (Portugal), was evaluated by using the Faro Focus 3D 120
31 Laser Scanner.

33 **Keywords:** Historical constructions; Masonry construction; Damage mapping; Construction
34 diagnosis; Terrestrial Laser Scanner; Radiometric classification; Geometric features.

35 **1 Introduction**

36
37 Currently, Cultural Heritage (CH) is considered not only a keystone in the economic development
38 of a country but also a living witness of our age-old traditions [1]. For this reason, it is necessary
39 to safeguard the authenticity and integrity of our Cultural Heritage for future generations [2].

40 Inside the wide variety of constructions that compose our CH assets, from religious buildings [3],
41 to network infrastructures [4] or rock art manifestations [5], masonry is the most commonly used
42 constructive solution. This popularity arises from its resistance to degradation agents compared
43 with other materials such as wood or adobe [6,7]. However, the other constructive systems,
44 biological colonization, salts, and moisture among others [8] can promote the deterioration of the
45 ornamental pieces presented on the monument as well as a reduction of its service life [9].

46 Based on these considerations, several international documents such as the Venice or Krakow
47 Charters [2,10] demand the use of rigorous multidisciplinary approaches to study the conservation
48 state of our cultural legacy. The final aim is to preserve its authenticity and values and design
49 suitable restoration strategies to preserve the monument through time according to some modern
50 restoration principles [11].

51 The non-contact and accurate nature of Terrestrial Laser Scanners (TLSs) as well as the fast and
52 dense data acquisitions place these sensors as one of the best solutions for the 3D digitalization
53 [12] of CH assets. The 3D models obtained with these geomatic sensors are normally used to
54 create complex CAD models for further structural evaluation [4,13,14] or used to extract
55 elevations or section maps [15]. However, the potential of these sensors goes beyond a massive
56 register of spatial coordinates, since they also store very useful radiometric information, the
57 backscattered intensity data [16]. Using the combination of these two capabilities (radiometric
58 and geometric), a laser scanner can be positioned as one of the most versatile tools to remotely
59 study the conservation state of historical construction. In this way, a damage assessment can be

60 performed in three dimensions with the advantage of being able to quantify the damages mapped
61 on the monument in contrast with more traditional practices of manual damage mapping on
62 orthoimages or sections [15,17].

63 Under this assumption, this paper proposes a methodology to analyse together the radiometric
64 and geometric data captured by TLS systems. The final goal is to develop a method capable of
65 mapping a wide range of the most common damages of historical masonry construction promoted
66 by the presence of chemical, biological and physical alteration agents. To validate the proposed
67 strategy, a historical construction inside the Fortress of Almeida, in Portugal, was chosen as a
68 case study: the San Francisco Master Gate.

69 Within this context, the paper has been organized as follows: Section 2 defines the sensor used to
70 diagnose the state of conservation as well as the processing methodology that was followed;
71 Section 3 describes the Almeida Fortress and the San Francisco Master Gate; Section 4 shows the
72 results after applying the proposed methodology, and finally, Section 5 summarizes the
73 conclusions arising from the use of TLS data to analyse pathologies of historical constructions as
74 well as some future work.

75 **2 Methodology for exploiting radiometric and geometric data from TLS point clouds**

76 **2.1 Terrestrial Laser Scanner**

77 Due to the difficulty in accessing some parts of the case study as well as the unfavourable lighting
78 conditions (shaded and lighted areas) to perform the data acquisition in some parts, the use of a
79 TLS is the best solution given its active nature (independent of solar lighting conditions) and
80 versatility. Specifically, the Faro Focus 3D 120 (FF3D120) (Figure 1) was the sensor used to
81 evaluate the methodology proposed in this paper. The most relevant features of this TLS are
82 specified in Table 1.

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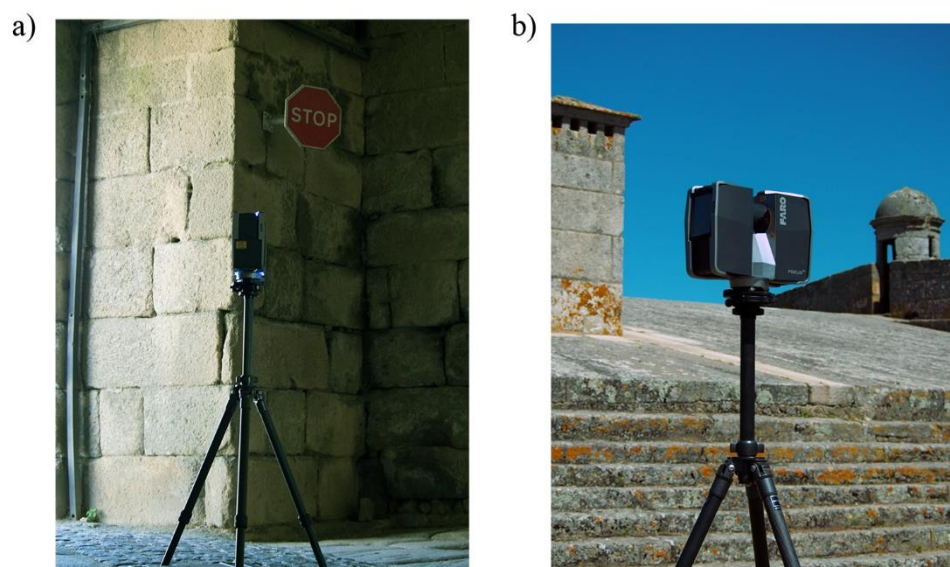
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Table 1: FF3D120 technical specifications.

Physical principle	Phase shift
Wavelength (nm)	905 - near infrared
Measurement range (m)	0.6 - 120
Field of view (degrees)	360 H x 320 V
Accuracy nominal value at 25 m (mm)	2
Beam divergence (mrad)	0.19
Capture rate (points/sec)	122,000 / 976,000
Spatial resolution at 10 m (mm)	6
Radiometric resolution (bits)	11

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Figure 1: TLS system during the data acquisition: (a) inside the barrel vault and (b) on the roof

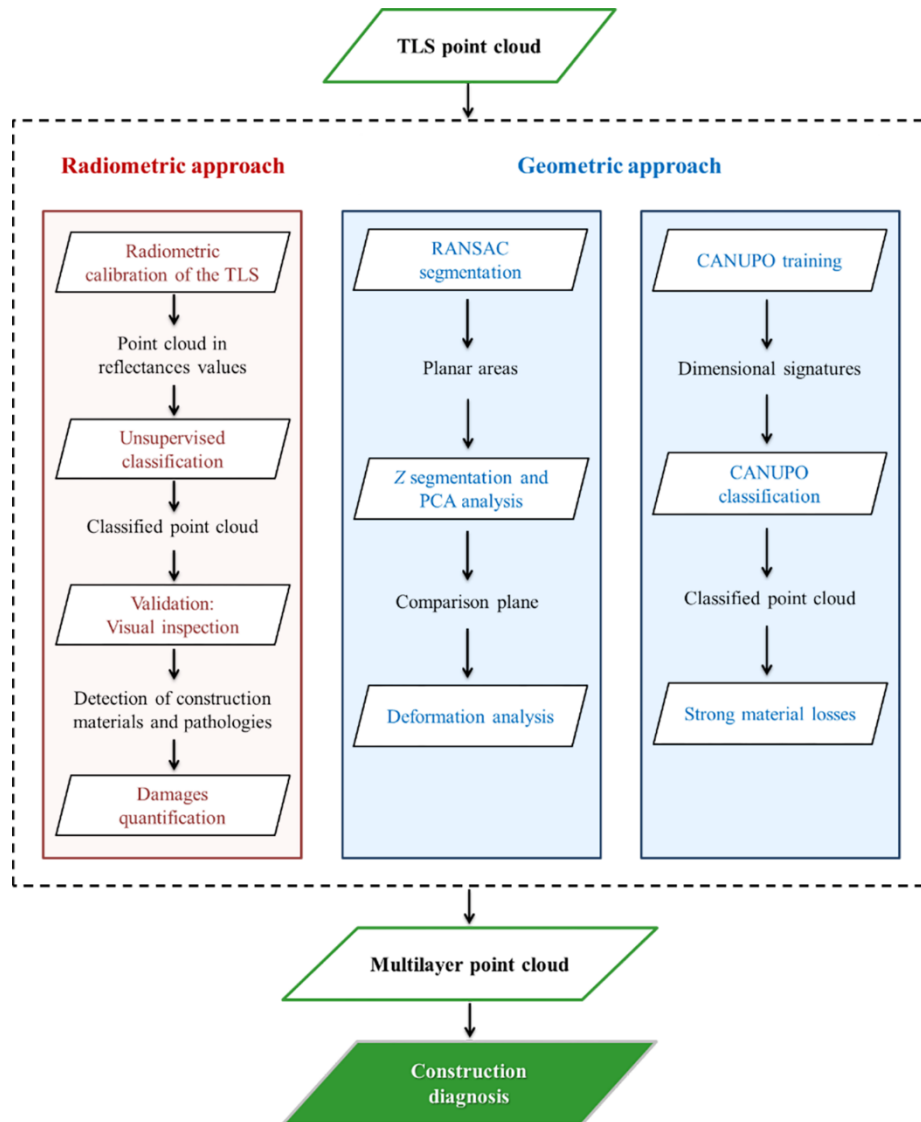
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91 2.2 Processing of laser scanner data for damage detection

92

3 To make full use of the TLS data acquisition for damage detection, we have decided to exploit the dual applicability of this sensor, radiometry and geometry laser data. For that reason, the laser point cloud takes two different paths in the processing step, the red- and blue-shaded areas of Figure 2. This figure summarizes the processing workflow followed to finally obtain a complete diagnosis of the state of degradation of construction.

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Figure 2: Scheme of the workflow followed to perform the mapping and evaluation of pathologies in the constructions.

100

101 The radiometric approach encompasses four processes: the radiometric calibration of the laser

102 scanner, an automatic classification of the point cloud to map different pathologies, the validation

103 of the classification by a visual inspection and the final quantification of damages. For its part,

104 the geometric approach encompasses two parallel processes: on one hand, a planar extraction by

105 means of the RANSAC shape detector, a z segmentation of the planes extracted to create the

106 comparison plane and the analysis of the discrepancies between the planar clusters extracted and

107 the comparison planes; and on the other hand, the CANUPO algorithm was trained and applied

108 on the point cloud to evaluate those areas with strong material losses. Finally, with the results of

109 both approaches, a multilayer point cloud was created to make a comprehensive and rigorous
110 diagnosis of the chosen construction considering both radiometric and geometric criteria.

111 **3.1 Pre-processing**

112
113 Historical constructions are geometrically characterized by their complexity and size, making
114 necessary the use of several scanning positions to record the whole construction. Considering the
115 complexity and size of the construction, the present methodology applied a coarse to fine strategy
116 to register the different scans taken [14]. First, a pairwise alignment, by means of the Iterative
117 Closest Point (ICP) algorithm [18], was used. Later, and with the aim of minimizing the error
118 accumulation, a global registration based on the Generalized Procrustes Analysis (GPA) approach
119 [19] was carried out. In this way, a dense and accurate 3D representation of the monument was
120 obtained.

121 With the 3D representation of the monument, the next step required to diagnose the construction
122 involves the extraction of the damage by the radiometric and geometric approaches proposed. In
123 accordance with the visual indicators proposed by ICOMOS [8], the following pathological
124 processes were evaluated: (i) deformations, (ii) disaggregation, (iii) biological activity, (iv) salt
125 crust and (v) moisture.

126 **3.2 Radiometric approach**

127
128 Backscattered laser intensity generates very useful radiometric information to evaluate the object
129 not only quantitatively but also qualitatively [16,20]. In this way, by using a single sensor, it is
130 possible to perform very comprehensive and rigorous studies of the construction from which to
131 derive both deformation and structural analysis as well as characterize visual indicators of
132 degradation such as biological colonization or crusts.

133 In addition, if the laser intensity data are radiometrically calibrated, the range of studies will be
134 broadened, allowing quantity and quality multitemporal analysis of the construction. In this
135 procedure, the raw intensity laser signal (in digital values) is transformed into surface reflectivity

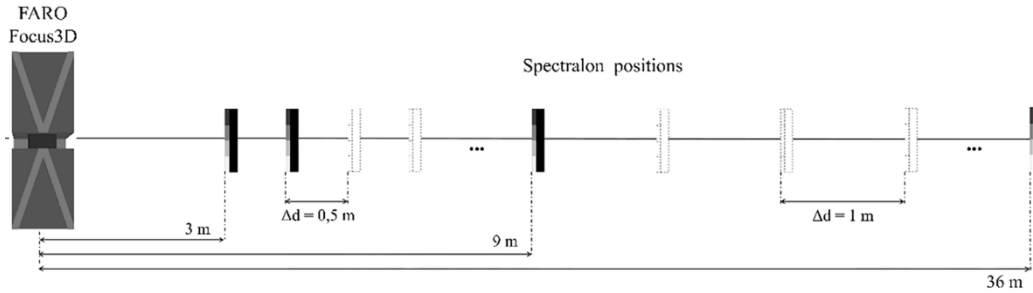
136 values. These values are inherent characteristics of each material (related to their physical
137 properties), and thus, it is possible to define each one unequivocally. Thus, any alteration of a
138 material will result in a change in the way the material reflects incident radiation and will therefore
139 be captured by the sensor.

140 During the radiometric calibration, the following factors are considered globally relevant in the
141 backscattered laser signal behaviour [21]: (i) the scanning geometry, (ii) the surface properties of
142 the materials, and (iii) some instrumental parameters.

143 Two factors define the scanning geometry: (i) the distance between the scanner and the object,
144 and (ii) the incoming beam incidence angle to the object [22,23]. The distance effect plays a strong
145 role in TLS and consists of an attenuation proportional to the square of the distance considered
146 usual. However, the two factors must be studied individually for each specific scanner since the
147 instrumental effects depend on each specific device [24-26]. However, the incidence angle effect
148 is related not only to the scanning geometry but also to the scattering properties of the object
149 surface [27].

150 **3.2.1** *Radiometric calibration of the TLS*

151
152 The FF3D120 was calibrated in a previous field campaign [9] for the range of distances between
153 9 and 36 m. This range has been extended from 3 to 36 m to use the calibrated laser intensity in
154 field campaigns where a greater proximity to the object of study is required, as in the case study
155 covered by this paper. Specifically, a reflectance-based radiometric calibration [28] consisting of
156 analysing the distance-behaviour of the backscattered TLS radiation was performed by using the
157 same equipment and methodology as was used in the previous experiment. Under laboratory
158 conditions and in a completely dark room, a 4-panel Spectralon® was stationed at 0.5 m intervals
159 from 3 to 9 m to be scanned (Fig. 3) at a resolution of 6 mm at 10 m to complete the range of
160 distances of the previous calibration [16].



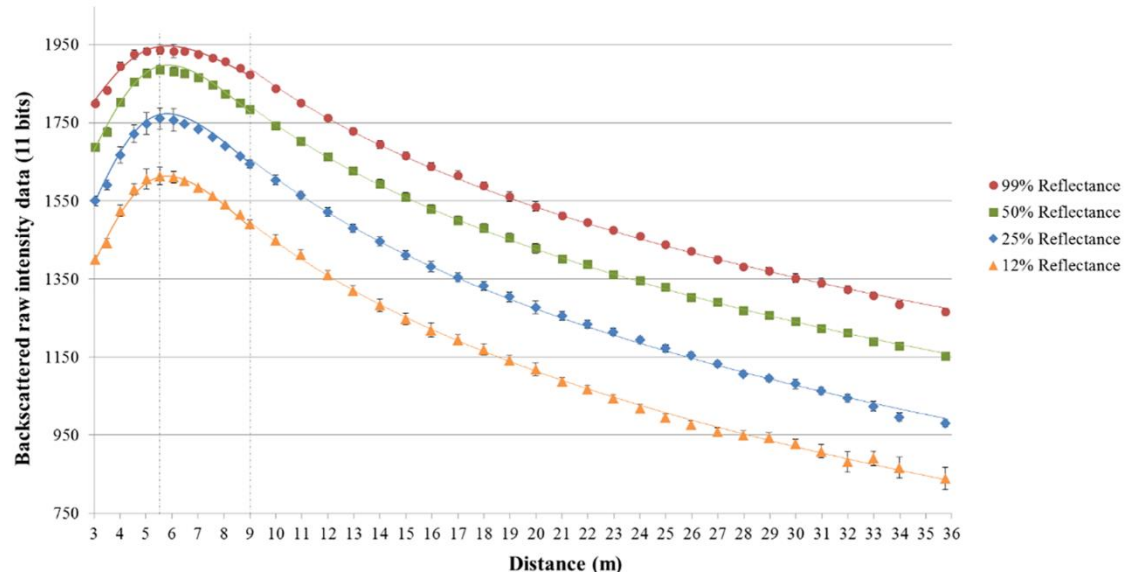
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163 **Figure 3:** Illustration of the FF3D120 data acquisition design to study the behaviour of the backscattered intensity
164 regarding different scanning distances.

165

166 Raw intensity data belonging to each reflectance panel (99%, 50%, 25% and 12% reflectance)
167 were calculated by averaging the intensity values associated with the group of points belonging
168 to each panel. Finally, the internal behaviour of the FF3D120 was modelled by comparing the
169 mean intensity value per panel with the distance at which each acquisition was made, resulting in
170 the graph illustrated in Figure 4.

171



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174 **Figure 4.** FF3D120 backscattered intensity behaviour with distance. Measurements from a 4-panel Spectralon placed
175 at different distances increments.

176

177 For this range of distances, the logarithmic behaviour of the FF3D120 backscattered intensity data
 178 was adjusted using the next empirical equation (Eq. 1).

$$\rho_{range} = e^{a \cdot d} \cdot b d^2 \cdot e^{c_1 \cdot I_F} \quad (1)$$

179 **Table 2.** Empirical coefficients obtained during the calibration campaign carried out.

Range of distances	a	b	c ₁	R ²
3-5.25	-1.0928	3.029510 ⁻⁵	0.006397	0.9868
5.25-9	-0.1134	4.944610 ⁻⁷	0.005911	0.9932
9-36	0.0214	3.907210 ⁻⁷	0.005415	0.9966

180
 181 Table 2 shows the coefficients obtained for the calibration of the FF3D120, where *a* and *b* are
 182 two empirical coefficients related to the signal attenuation and internal conversion from the
 183 received power to the final digital levels, *d* is the distance between the laser scanner and the
 184 measured object, *c₁* is the gain of the TLS and *I_F* is the raw intensity data in digital levels (11
 185 bits).

186 Once the calibration is done, the intensities of points corresponding to the proportion of radiation
 187 reflected by each surface are expressed in reflectance (% of reflected radiation) instead of digital
 188 levels.

189 **3.2.2** *Incidence angle affectation*

190
 191 The incidence angle (*α*) of the laser beam is an important factor that affects the received intensity
 192 according to Lambert's Law [29]. The incidence angle is defined as the angle between the surface
 193 normal, obtained through the Principal Component Analysis of the surface (PCA), and the
 194 incoming laser shot ray. For ideal Lambertian scatters, the reflected intensity is proportional to
 195 *cos α*. The higher the incidence angle of the laser beam, the smaller the amount of light coming

196 back to the sensor. In this study, due to the lack of information about the reflection characteristics
197 (BRDF index) of each of the materials to be measured, it has been assumed that all the surfaces
198 have a Lambertian behaviour.

199 By applying the following equations (Eq. 2 and 3), it is possible to correct the backscattered laser
200 radiation from the incidence angle affectation considering for this purpose the surface normal,
201 calculated during the pre-processing phase (Section 2.2.1).

$$\rho_{905nm} = \frac{\rho_{range}}{\cos \alpha} \quad (2)$$

202

$$\alpha = \arccos \frac{\vec{u} \cdot \vec{v}}{|\vec{u}| \cdot |\vec{v}|} \quad (3)$$

203

204

205 where \vec{u} is the normal vector to each point of the point cloud, \vec{v} the beam-directing vector and $|\vec{u}|$
206 and $|\vec{v}|$ the magnitude of each vector.

207 **3.2.3** *Classification procedure*

208 For the pathological evaluation through the radiometric approach, an automatic clustering
209 categorization has been performed to group 3D point clouds in different “clusters” [30] by
210 analysing, in this case, the calibrated intensity data (reflectance) through an unsupervised
211 classification method. Thus, points that are grouped together have reflectance like each other.

212 A variety of algorithms perform this kind of classification. The Fuzzy K-means clustering
213 algorithm [31], one of the most widely used and the one being used in this work, consists of
214 minimizing the squared distance between feature values of two points that reside in the same
215 cluster. The approach on which the centre of each cluster is solved finds the minimum of a sum-
216 of-squares cost function (Eq. 4) using coordinate descent.

$$J_q(U, V) = \sum_{j=1}^N \sum_{i=1}^K (u_{ij})^q d^2(X_j, V_i); \quad K \leq N \quad (4)$$

217 where q is any real number greater than 1 and is the weighting exponent for u_{ij} that controls the
 218 “fuzziness” of the resulting clusters, U is a $N \times K$ partition matrix where N is the number of data
 219 points and K the number of clusters, $V = \{V_1, V_2, \dots, V_K\}$ is a set of objects in the same object
 220 domain, X_j is the j^{th} m -dimensional feature vector, V_i is the centroid of the i^{th} cluster, u_{ij} is the
 221 degree of membership of X_j in the i^{th} cluster and $d^2(X_j, V_i)$ is any inner product metric (distance
 222 between X_j and V_i).

223 Fuzzy partitioning is carried out through an iterative optimization of the cost function shown
 224 above (Eq. 4), with the update of membership u_{ij} and the cluster centres \hat{V}_i by Eq. 5

$$u_{ij} = \frac{\left[\frac{1}{d^2(X_j, V_i)} \right]^{1/(q-1)}}{\sum_{k=1}^K \left[\frac{1}{d^2(X_j, V_k)} \right]^{1/(q-1)}}, \quad \hat{V}_i = \frac{\sum_{j=1}^N (u_{ij})^q X_j}{\sum_{j=1}^N (u_{ij})^q} \quad (5)$$

225 This iteration will stop when $\max [|u_{ij} - \hat{u}_{ij}|] < \varepsilon$, with ε as a termination criterion between 0
 226 and 1. This method converges to a local minimum or a saddle point of J_q .

227 3.3 Geometric approach

228 Complementary to the radiometric data acquired by TLS systems, geometrical features stored in
 229 the point cloud, such as normals or the dimensionality of the points, can be used to detect
 230 additional pathological processes such as deformations or material losses.

231 The deformation evaluation can be carried out following two approaches [17,32]: (i) direct point
 232 to point comparison and (ii) point to primitive distance evaluation. Regarding the first approach,
 233 at least two point clouds are required to compare different states. Meanwhile, the second approach
 234 requires a point cloud segmentation into different components. Components that later are fitted
 235 to primitives and compared with the original point cloud. Considering the lack of previous data,

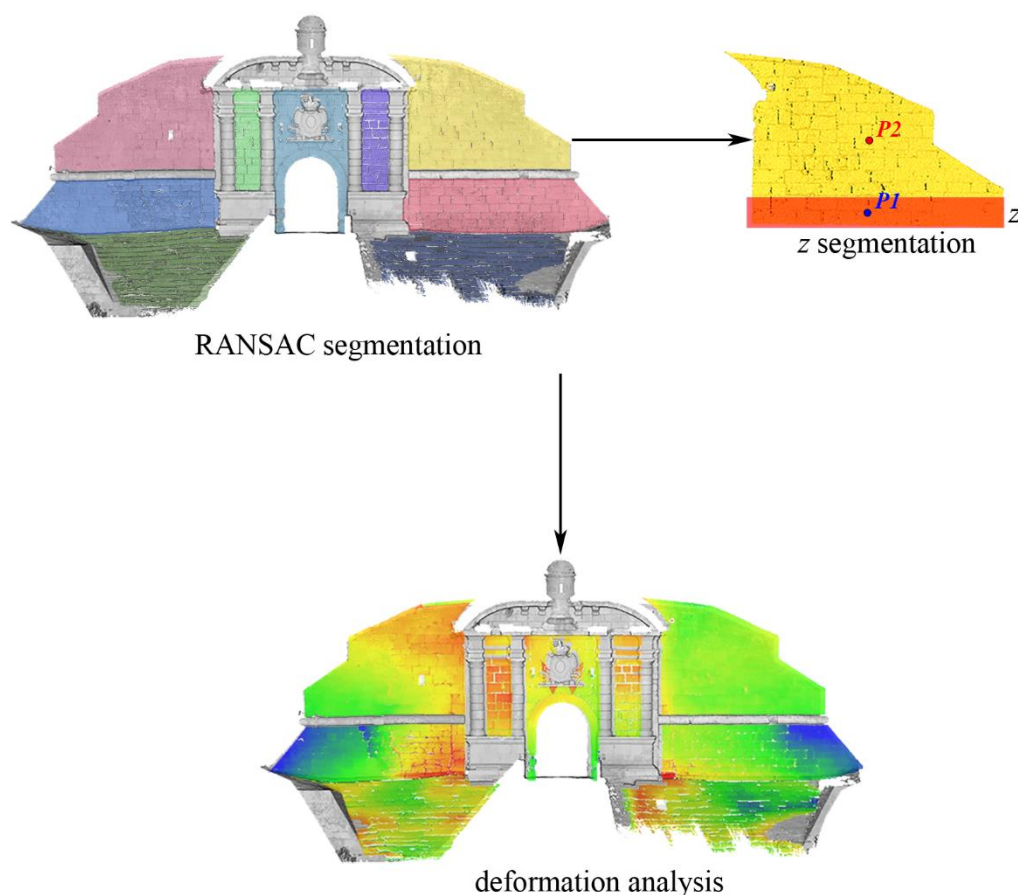
236 the second approach was used to estimate the deformation of different elements of the
237 construction.

238 Inside the wide variety of constructive elements present in a historical building, planes (façades
239 or roofs) are one of the most common primitives. Therefore, a suitable strategy was necessary to
240 extract all the points in the point cloud and affect them to a particular primitive. For this purpose,
241 the RANSAC Shape Detection algorithm [33] was used.

242 However, primitives extracted by means of the RANSAC algorithm cannot be considered
243 representative, being influenced by the current deformation state (considering that the plane
244 extracted was initially a perfectly plane). To minimize this influence, a z segmentation was carried
245 out to extract all those points between two z values (e.g., points that belong to the first two rows
246 of masonry blocks) followed by a Principal Component Analysis (PCA) to extract the maximum
247 dispersion and the centroid of these points (façade direction). Finally, a reference plane was
248 created with the maximum dispersion vector, the centroid, as well as a second point obtained by
249 sifting the z value of the centroid (Fig. 5).

250 For the case of non-vertical planes (e.g., roof planes) and during the z segmentation stage, an
251 additional PCA analysis was carried out to align the minimum (normal vector) and maximum
252 dispersion directions with the x and y -axis, respectively.

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256 **Figure 5:** Graphical representation of the workflow followed to evaluate the deformations in the façade.

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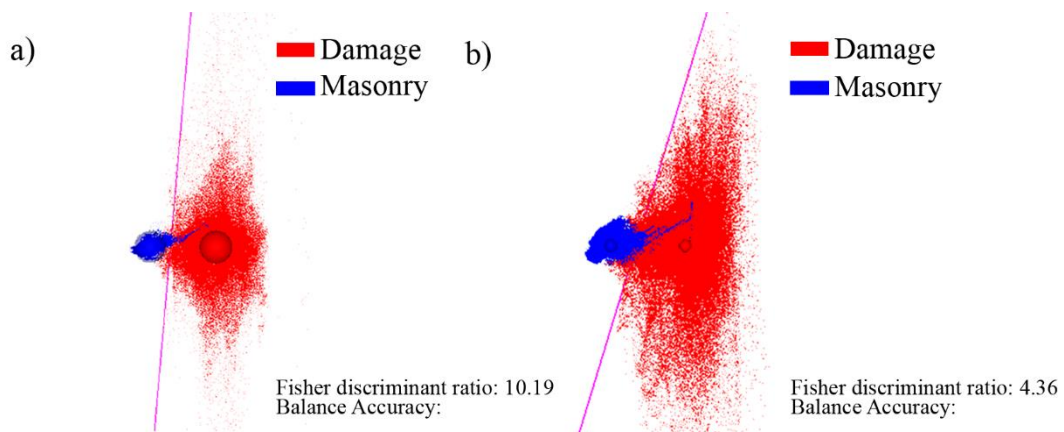
258 However, material disaggregation is a common pathological process in masonry constructions for
259 which the procedures defined previously cannot provide a suitable solution.

260 Generally, at the block scale, simple masonry constructive elements such as barrel vaults can be
261 interpreted as planar surfaces. Meanwhile, the loss of material can be interpreted as a local 3D
262 feature. Thus, the analysis of the dimensionality of the point stands as a possible solution to
263 characterize the pathological process. Considering this analysis, the CANUPO algorithm [34] was
264 applied to detect those areas with a strong lack of material, comprising the following stages: (i) a
265 first training phase, and (ii) a final classification stage.

266 During the training phase, several local dimensionality analyses were carried out to characterize
267 the point cloud at different scales (1D dimensionality indicates that points at this scale belong to
268 a line, 2D to a planar surface and 3D to a volumetric surface). Finally, a Linear Discriminant
269 Analysis is applied to find the hyperplane of the maximal class separability [34] (Fig. 6).

270

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274 **Figure 6:** Results during the CANUPO training: (a) Classifier A; (b) Classifier D. In red is the damage class, in blue
275 masonry and in magenta the hyperplane of maximal separability.

276

277 Once the classifier is trained, points can be clustered into one of the two predefined classes during
278 the training stage, allowing the segmentation of the point cloud. For the present case study, the
279 predefined classes were masonry and damages.

280 **4 Case study: Almeida Fortress**

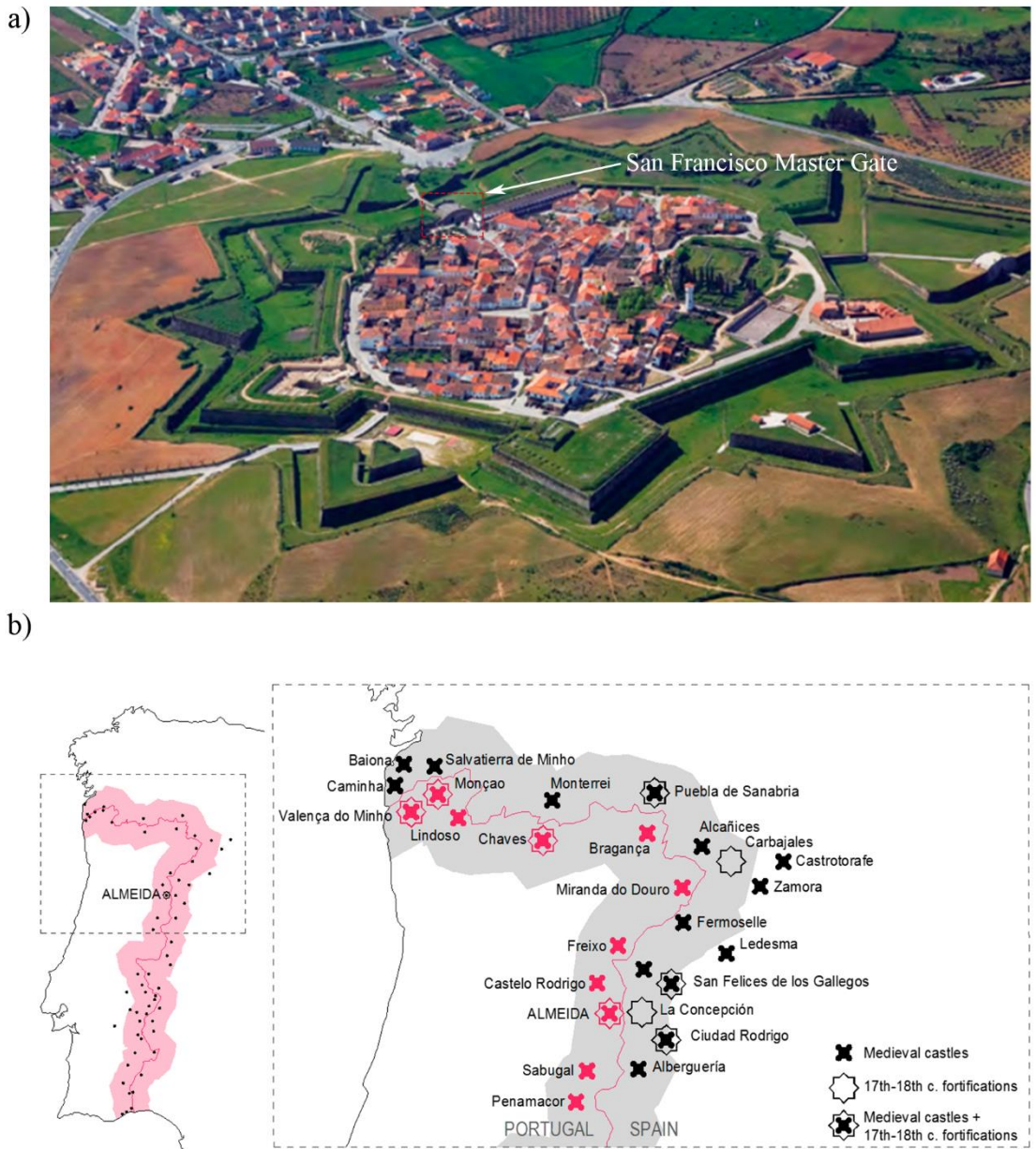
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282 The Fortress of Almeida is a bulwarked fortification that, although it has been classified as
283 “National Monument” since February 1928, wishes to break barriers, clearing the path that leads
284 to a global projection as a UNESCO World Heritage site [35].

285 The desire for conservation of the heritage in Almeida is evident because not only has part of the
286 ruined heritage been recovered, but also, the priority has been given to give new life to these
287 spaces, transforming them into museums, offices and diverse spaces for the benefit of the
288 community. This determination was based on several initiatives: seminars, research work,
289 protocols with universities and technical schools that have given shape, step by step, to a sense of
290 sustainable safeguarding [35].

291 **4.1 Historical background**

292 The Fortress of Almeida, composed of six bastions that form a star, is in the heart of the historical
293 city of Almeida near the city of Guarda, Portugal (Fig. 7a). This military infrastructure was
294 erected on the east side of the Côa River, and due to its strategic location, the city was condemned
295 to be a place of war (Fig. 7b).



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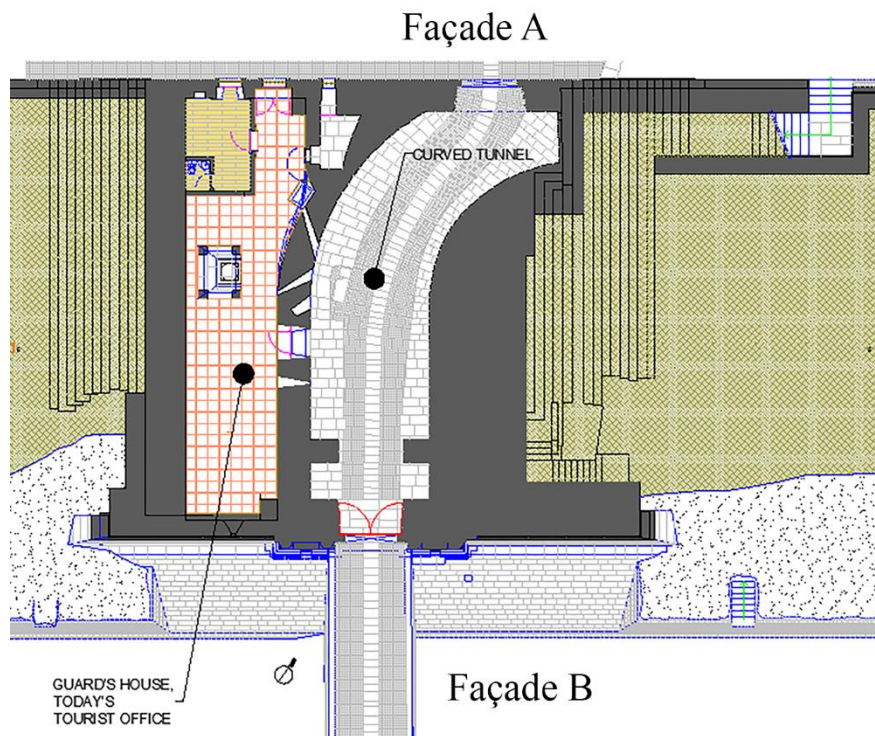
297 **Figure 7:** Location of the Almeida fortress: (a) Aerial view of the Almeida fortress [4] and (b) Spatial disposition of
298 the military fortifications along the border between Spain and Portugal, based on [36] and [37].

299

300 In the Middle Ages and until 1297, Almeida was a space for dispute between Christians and
301 Muslims. Later, the city was a victim of constant sieges and attacks due to the conflictive climate
302 that appeared after the independence from the Castilian Kingdom of Leon during the 13th century
303 [35]. During these tormented periods, the fortress was the focus of several constructions,
304 demolitions and reconstructions. For more details, see [36].

305 4.2 The Master Gate of San Francisco

306 Placed as one of the Master Gates of the Almeida fortress, the construction of the Gate of San
307 Francisco began between 1661 and 1667. The geometry of the wall was envisioned in such a way
308 that the inclination angle made projectiles bounce in the direction of the enemies, and the massive
309 amount of earth acted as a cushion partially absorbing the impact of projectiles [35]. Regarding
310 the structural composition, two parts can be highlighted (Fig. 8): (i) a curved barrel vault that acts
311 as a tunnel, allowing the transit into the city, and (ii) a lateral camera, which used to be the house
312 of the guard. This second section is believed to have been added between 1744 and 1789. Also
313 during this period, restoration works were carried out to replace damaged stones with new ones.

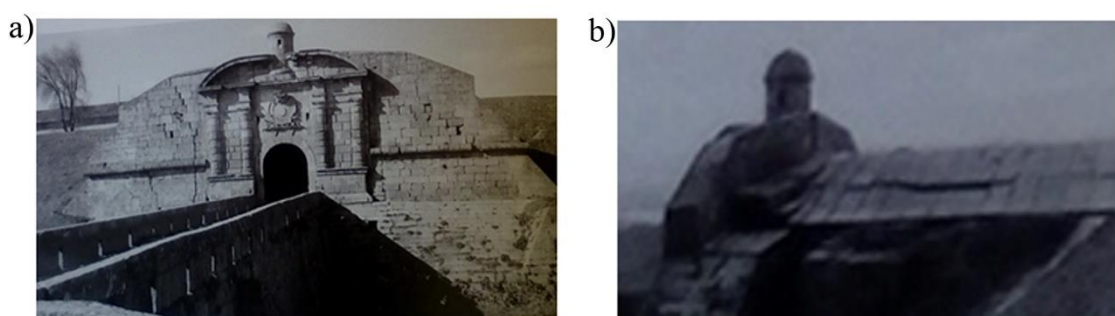


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315

Figure 8: Plant view of the San Francisco Master Gate.

316 The French invasion in 1810 will pass down in history as the most destructive event both for the
317 fortress and the Master Gate of San Francisco. The constant bombing and the explosion of the
318 gunpowder storehouse destroyed the castle and generated great damage to the fortress and
319 specifically to this Master Gate. By 1815, the order to start reconstruction work on the Gate was
320 issued, although since the war ended in 1814, the urgency of reconstruction was low and the
321 construction works were kept to a minimum. It was not until the 1960s that a significant
322 restoration project occurred (Fig. 9).



324 **Figure 9:** State of damage in the Master Gate of San Francisco in 1962: (a) façade B with vertical cracks and loss of
325 material; and (b) crack on the roofing system (stone roof).

326

327 In 1986, work continued in the San Francisco Master Gate, where the right side urgently needed
328 consolidation and cleaning of the masonry. The mortar used during this restoration was a
329 hydrophobic mix with cement with an estimated proportion of 1:2/3:6 (cement:lime:sand) [35].
330 Figure 10 shows its current aspect.

331



332

333

334

Figure 10: Current aspect and state of conservation of the San Francisco Master Gate [4].

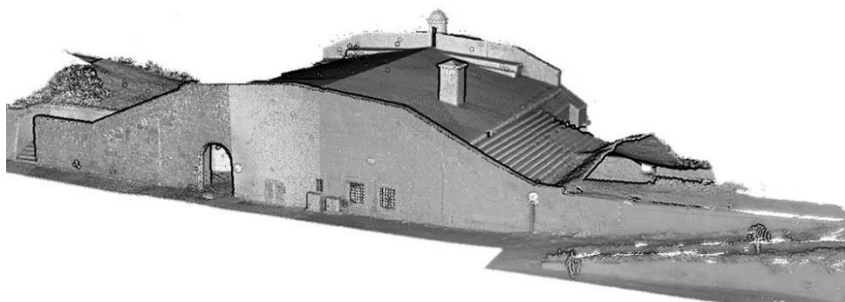
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336 5 Damage mapping results

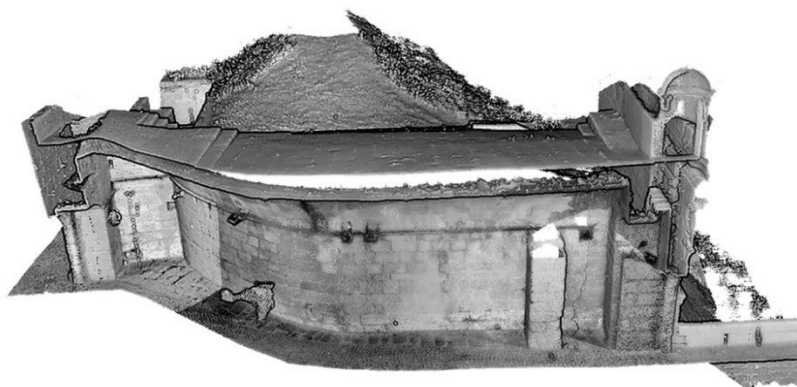
337 5.1 Data acquisition: San Francisco Gate scenario

338 To build the 3D model of the Gate, twenty-six scans were needed to capture the whole structure:
339 (i) eleven scans to represent the façades, (ii) five stations to capture the barrel vault, and (iii) ten
340 scans to represent the roof of the construction. The huge amount of data captured, with a total of
341 712,324,286 points, required an optimization of the point cloud for further evaluations. Therefore,
342 two filters were applied previously to the registration stage: (i) distance filter with an average
343 threshold of 15 m, and (ii) a density filter to delete all the points that have neighbours closer than
344 5 mm. Then, the coarse to fine registration strategy defined in Section 2.4 was carried out. As a
345 result, a complete and accurate 3D representation of the Gate was obtained, composed of
346 104,451,530 points (14% of the original point cloud), with a registration error of 0.005 ± 0.003
347 m (Fig. 11).

a)



b)



348

349 **Figure 11:** Registered point cloud: (a) Isometric view of the San Francisco Master Gate; (b) Longitudinal section
350 across the barrel vault.

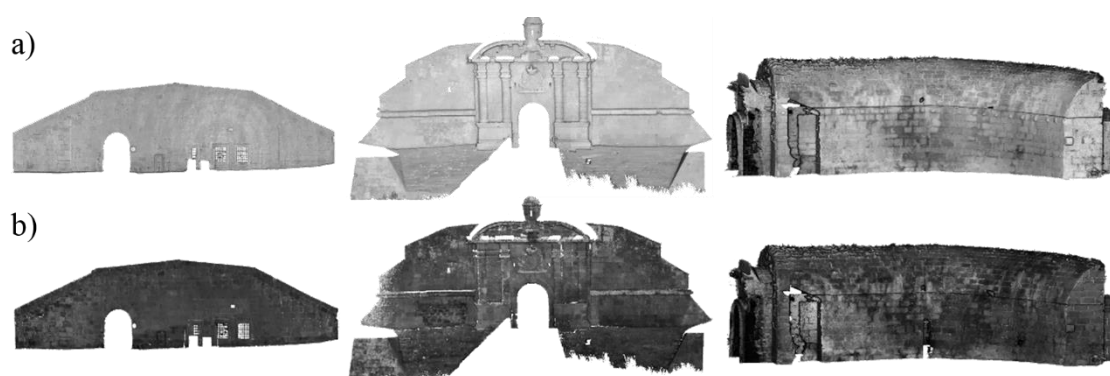
351 Considering the results provided by a visual inspection, the following constructive elements were
352 evaluated: (i) façades A and B, (ii) roof, and (iii) barrel vault through the approaches defined in
353 Section 2.

354 5.2 Results of the radiometric approach

355 5.2.1 Point cloud models in reflectance values

356 According to the methodology explained in Section 2 and illustrated in Figure 2, the
357 characterization of visual indicators of damage in the selected constructive elements (façades and
358 barrel vault) were evaluated. To that end, a radiometrically calibrated TLS was used to analyse
359 the backscattered intensity in surface reflectivity values instead of raw digital levels (Fig. 12).

360 Calibrated point clouds show a great difference in terms of contrast. In the raw point cloud,
361 radiometry is more homogeneous for the whole construction, and there are fewer differences
362 between materials and possible pathologies than in the calibrated models.



363
364 **Figure 12:** Comparison between the point clouds: (a) raw intensity data in digital levels and (b) in reflectance values
365 after applying the radiometric calibration.
366

367 Having 3D models in reflectance values offers many other advantages than better visual
368 appearance. On the one hand, they allow the evaluation of the evolution of pathologies through
369 time, because by correcting the raw intensity data, laser acquisitions become invariant by the
370 scanning geometry, that is, unaffected by the acquisition distance and the beam incidence angle
371 [22]. Finally, by analysing physical values (inherent to each material) instead of digital levels
372 provided by the internal electronics of the laser, studies become more rigorous, improving the
373 accuracy of the classification [26,29]. This last advantage also allows us to evaluate, by comparing
374 with available spectral libraries, whether the identification of materials and pathologies is more
375 or less accurate.

376 **5.2.2** *Classified point cloud*

377 To assess the potential of the proposed radiometric approach for detecting pathologies, three
378 automatic classifications of the models were performed, establishing four, five and six clusters.
379 Thus, the most suitable number of clusters for this dataset and for the wavelength of the laser
380 scanner (905 nm) was evaluated. The mean reflectance and its standard deviation for each of the
381 clusters were calculated according to the three unsupervised classifications performed. Finally,
382 five clusters were chosen as the best option since the separability between the clusters of this
383 classification was the optimum among the three performed (Table 3). In this case, a small overlap
384 of 1.25% occurred between cluster 4 and cluster 5 but was assumed to be acceptable (Fig. 13)
385 since it remains within the range of error estimated for this calibration technique (approximately
386 5%).

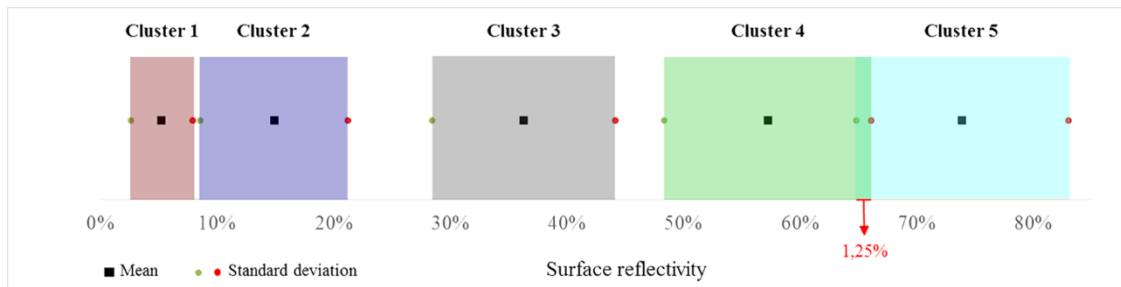
387 **Table 3.** Spectral behaviour of each cluster.

388

	Surface reflectivity (%)	
	Mean	Standard Deviation
Cluster 1	5.27 %	2.64 %
Cluster 2	14.91 %	6.31 %

Cluster 3	36.35 %	7.84 %
Cluster 4	57.25 %	8.86 %
Cluster 5	73.95 %	9.10 %

389



390
391
392

Figure 13: Graphical representation of the separability between clusters. It is worth mentioning the presence of a little overlap between cluster 4 and 5.

393

By applying the Fuzzy K-means clustering algorithm [31], each point of the point cloud was

394

coloured according to the more related cluster of the five established for the three constructive

395

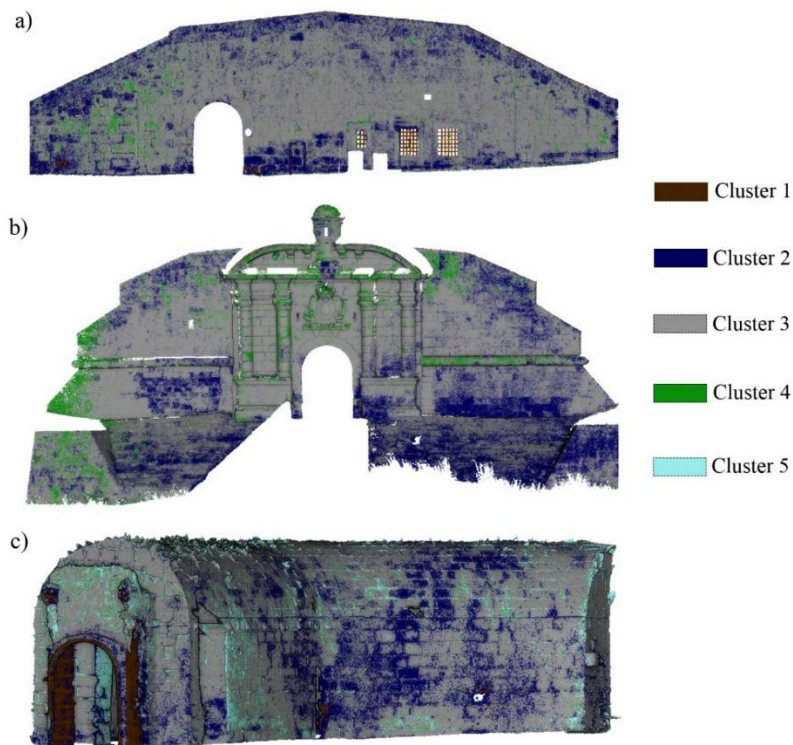
elements studied. As Figure 14 shows, in all three classified models, there were areas with some

396

pathologies. Taking a visual inspection of an expert into account, clusters were associated with

397

the construction material and/or pathology with real meaning.



398

399

Figure 14: Results obtained for the Fuzzy-kmeans unsupervised classification carried out: (a) façade A; (b) façade B;

400

and (c) barrel vault.

401 **5.2.3** *Validation of the classification and damages quantification*

402

403 To validate this methodology, a comparison between the analysis results and real photographs

404 (Fig. 15) was carried out. Comparing the five classified clusters with the informational classes

405 provided by an expert visual inspection, it is possible to make the following correspondences: (i)

406 Cluster 1 corresponds to wood or iron materials, (ii) Cluster 2 to humid areas and black deposits,

407 (iii) Cluster 3 to granite stones, (iv) Cluster 4 to areas with presence of any type of biological

408 colonization, and (v) Cluster 5 to salt crusts.

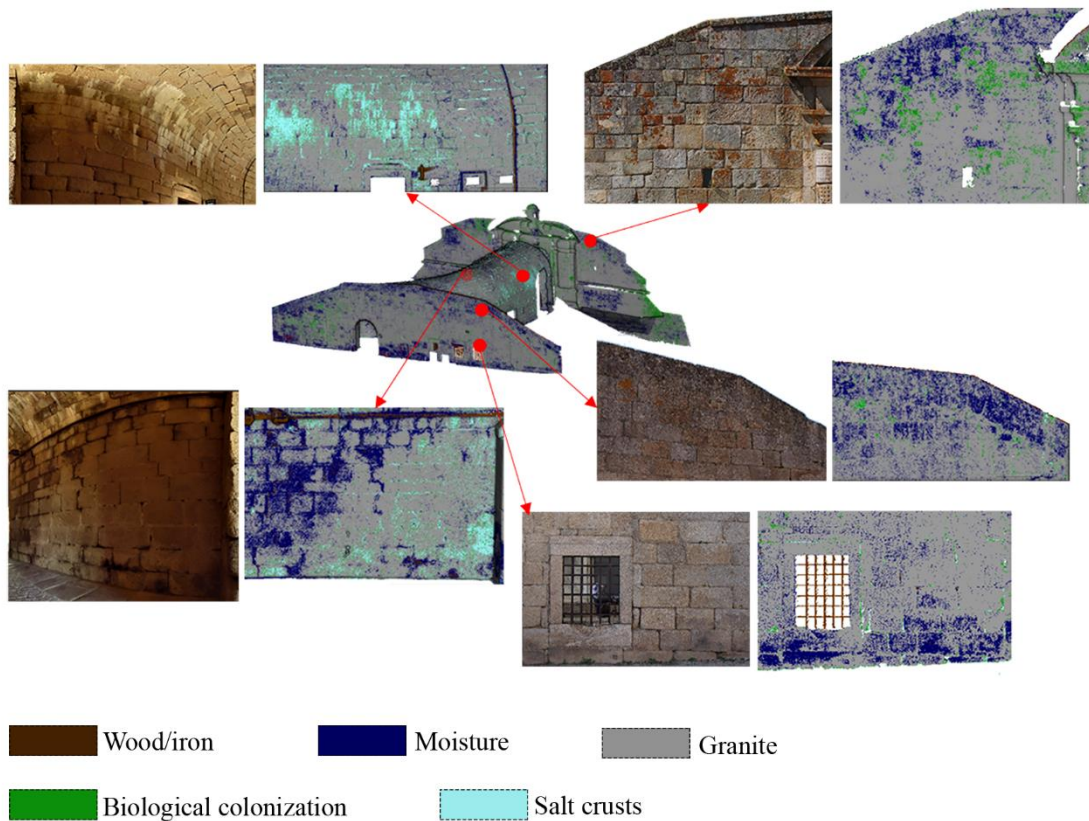


Figure 15: Validation and interpretation of the classification through an expert visual inspection.

Regarding wood and iron built-up surfaces, it was not possible to distinguish between them since they have a close surface reflectivity [40] of approximately $6\% \pm 3\%$ at the wavelength for which the FF3D120 operates (905 nm). Thus, areas with these construction materials were classified together among the same cluster.

417 Table 4 quantifies the percentage of each of the materials and pathologies detected for the three
418 analysed construction elements. The sum of points belonging to each cluster (expressed as a
419 percentage) regarding the total number of classified points is shown in this table.

420 **Table 4.** Proportion of each information class extracted during the radiometric evaluation.

Classes:	Façade A	Façade B	Barrel vault
Wood/Iron	0.95 %	0.08 %	2.28 %
Granite (undamaged)	80.43 %	81.42 %	71.37 %
Moisture	15.82 %	12.52 %	15.83 %
Biological colonization	2.32 %	5.96 %	2.67 %
Salts	0.48 %	0.02 %	7.85 %

421
422 Focusing on the pathological analysis, the results show that in the three analysed locations, there
423 is a high percentage of moisture (black deposit) (Fig. 15). In contrast, there is not a similar
424 presence of biological colonization or salts in the three constructions. Façade B presents a greater
425 affection for biological colonization (mainly orange lichens) due to its orientation, and the barrel
426 vault has a larger area affected by efflorescence than the rest.

427 **5.3 Evaluation of the geometric features: deformations and erosions**

428 **5.3.1 Deformations**

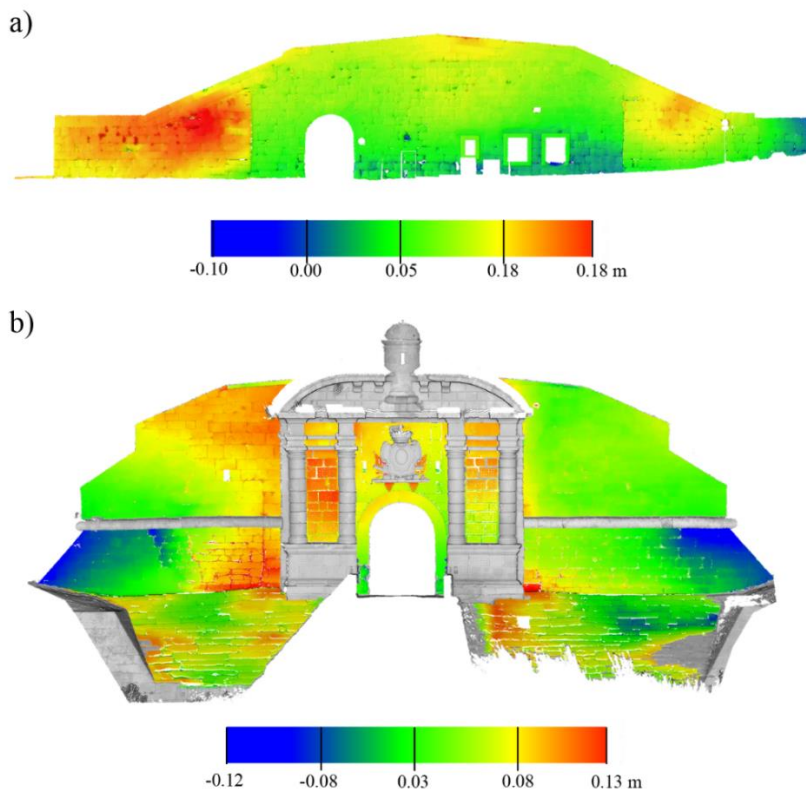
429 The next process aims to evaluate the current deformation state of the selected constructive
430 elements of the case study: (i) façade A, (ii) façade B, and (iii) roof, following the method
431 proposed in Section 2.5 with a z value of 0.80 m (a height of two masonry blocks).

432 Regarding façade B, several planes were obtained by means of the RANSAC shape detection,
433 requiring an additional clusterization process. This segmentation was based on the similarity, in
434 terms of plane normal and centroid position, between clusters (Fig. 16, 17 and 18).

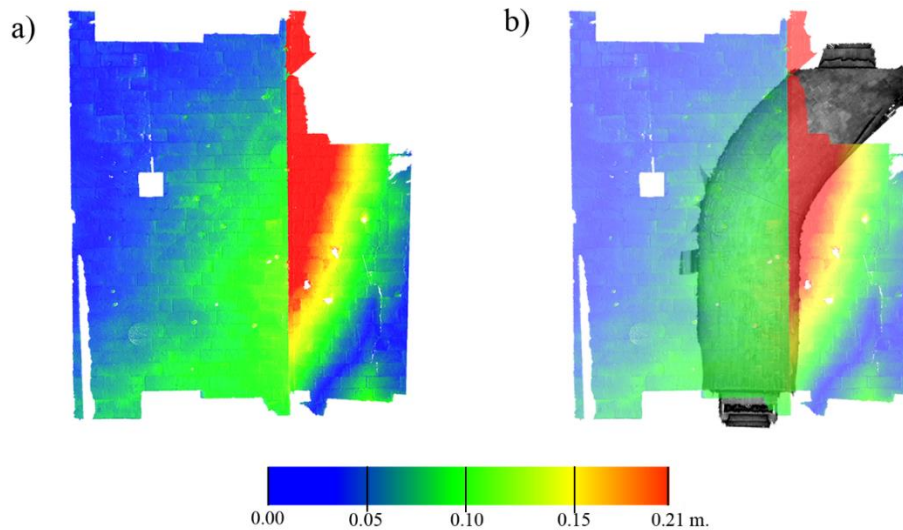
435



436
437 **Figure 16:** Segmentation carried out on façade B: (a) clusters obtained through the RANSCAC shape detector; (b)
438 planes clustered according with their similarity.



439
440 **Figure 17:** Results obtained during the deformation analysis: (a) façade A, with a unique vertical plane; and (b)
441 façade B with vertical and non-vertical planes.



442

443

Figure 18: Deformation analysis carried out on the roof: (a) graphical representation of the results obtained; (b)

444

relation between the roof's deformation and the barrel vault position.

445

446 5.3.2 Erosions

447

448 Results obtained after the radiometric approach carried out on the barrel vault highlight a strong
449 presence of salts and moisture (Fig. 19). These pathological processes, which promote the
450 blistering of the masonry blocks (especially on the joints), are characterized by a local change in
451 the dimensionality of the constructive element. Therefore, they require the use of an additional
452 strategy to characterize these areas (Fig. 19).

453

454

455

456

457 Considering this additional strategy, several CANUPO classifiers were trained, using for this
458 purpose the average dimensions of the masonry block (0.90×0.40 m) as well as different

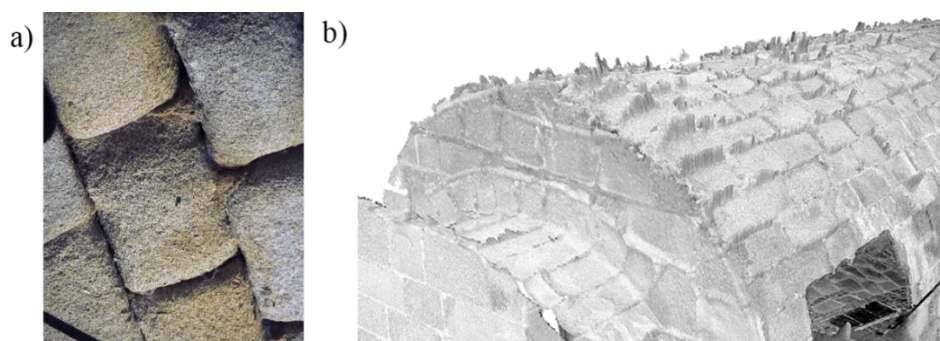


Figure 19: Block's blistering (a) Photo taken during the visual inspection; (b) Detail of part of the barrel vault point cloud.

456

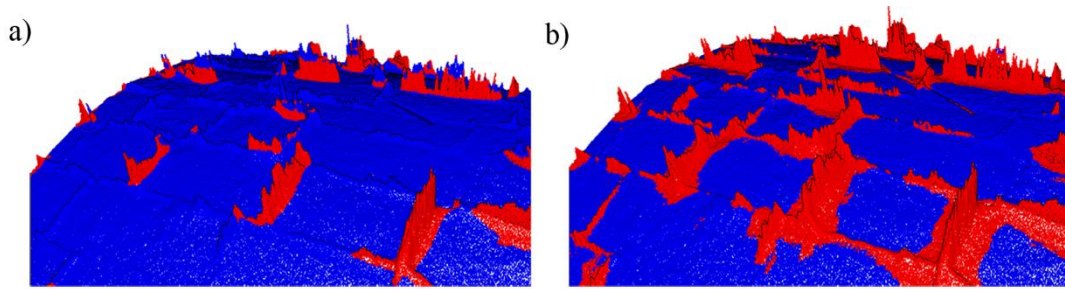
459 intervals (from 0.05 to 0.10 m) as possible work scales. Complementary, and with the aim of
 460 evaluating the performance of the algorithm, two quality analyses were used. On one hand, a
 461 quantitative evaluation was performed by means of the Balance Accuracy (*ba*) and the Fisher
 462 Discriminant Ratio (*fdr*) [20]. On the other hand, a qualitative analysis was performed through a
 463 visual evaluation of the results obtained (Table 5) (Fig. 20).

464 Classifier A shows the best qualitative and quantitative results (Table 4). However, it is possible
 465 to observe the presence of a high number of false negatives (Fig. 20a). This phenomenon arises
 466 from the block and the joint roughness on small scales, showing a dimensionality response similar
 467 to the eroded parts. According to this response, classifier A was tuned by manually changing the
 468 hyperplane position (classifier A_mod). This modification declined the quantitative indices
 469 (Table 5) slightly but, from the qualitative point of view, led to more accurate results (Fig. 20b).

470 **Table 5:** Performance of the CANUPO algorithm, at different configurations, in terms of Balance Accuracy and
 471 Fisher Discriminant Ratio.

Classification	Work scale			<i>ba</i>	<i>fdr</i>
	Maximum	Interval	Minimum		
A	0.90	0.05	0.05	0.99	10.19
B	0.90	0.10	0.05	0.99	7.80
C	0.40	0.05	0.05	0.97	6.91
D	0.40	0.10	0.05	0.96	4.36
A_mod	0.90	0.05	0.05	0.93	10.13

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480

481 **Figure 20:** Results obtained during the training phase, in red are the damage areas and in blue non-damaged areas:

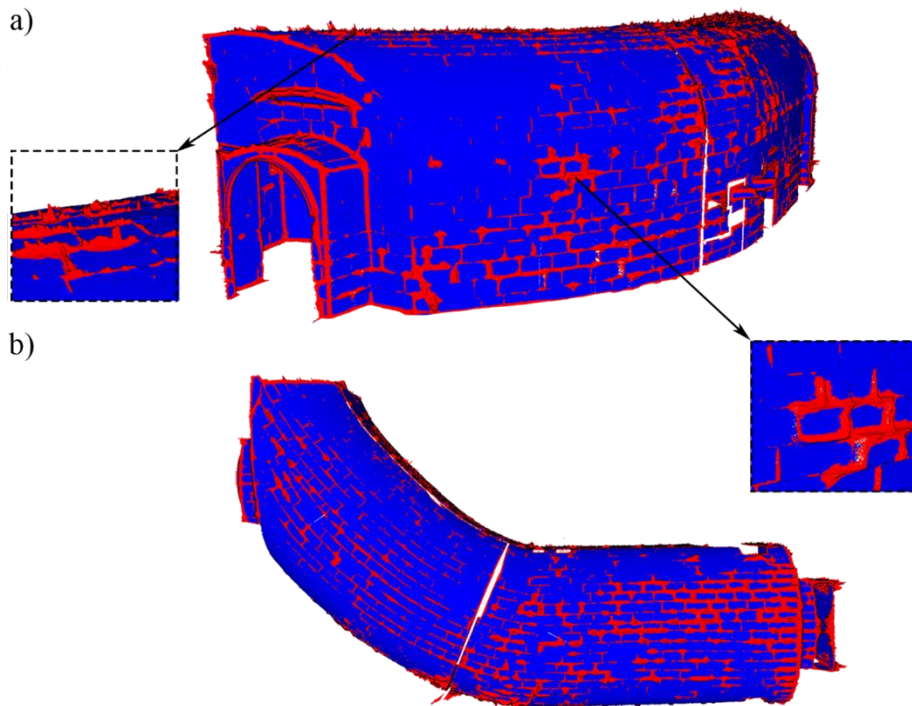
482

(a) Classifier A; (b) Classifier A_mod.

483

484 Considering the A_mod classifier as the most appropriate classifier, the whole barrel vault was

485 evaluated (Fig. 21).



486

487 **Figure 21:** Point cloud segmented by the A_mod classifier (in red are the damage areas, in blue non-

488

damage areas): (a) isometric and (b) plant view of the of the barrel vault.

489

490 In general terms, the CANUPO approach shows excellent correlation with the damage exhibited

491 on the barrel vault (Fig. 21a), highlighting the most eroded parts of the structure. However, some

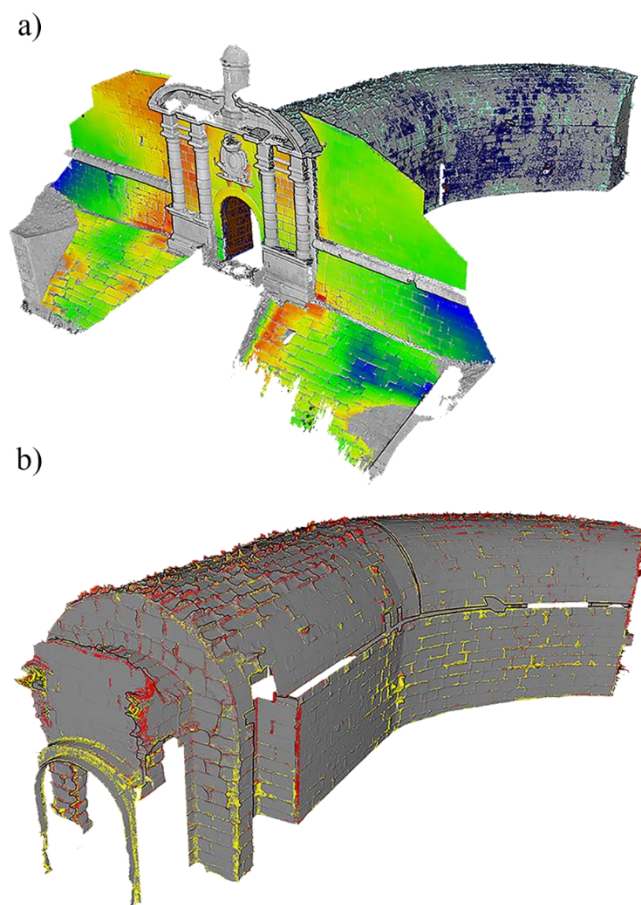
492 mismatches can be found on the edges of the point cloud as well as in the shadow areas, suggesting

493 the need to use additional filters to enhance the results obtained.

494 **5.4 Comprehensive approach to damage analysis: the multilayer point cloud**

495 At this point of the methodology, it has been possible to map a wide variety of pathological
496 processes through the different approaches defined and carried out by the proposed methodology.
497 Both radiometric and geometric methods add new layers of information to the original values of
498 the point cloud ($x, y, z, intensity$) referenced in the same coordinate system, allowing the creation
499 of a multilayer point cloud with information, not only about the geometric disposition of the
500 construction but also about the damage presented on the construction (Fig. 22a).

501 Considering the pathologies detected at the barrel vault, an analysis of the most important parts
502 (areas with strong erosion as well as the presence of moisture or salt crusts) was performed,
503 combining the results provided by the radiometric classification with the results obtained by the
504 CANUPO classifier (Fig. 22b).



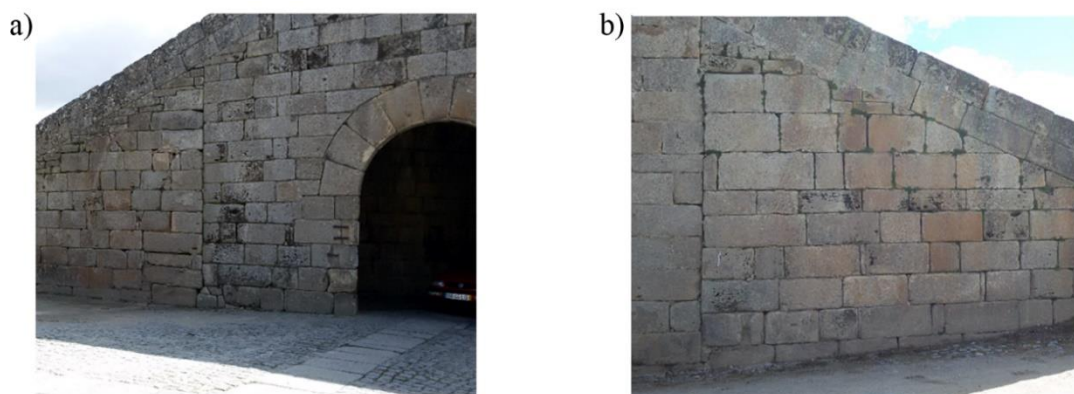
506 **Figure 22:** Multilayer point cloud: (a) isometric view with the deformation state of the façade B and the pathological
507 processes detected by radiometry on the barrel vault; (b) relation between pathological processes presented on the
508 barrel vault. In red, areas affected by strong erosions and salts, in yellow areas with erosions and moistures.
509

510 **5.5 Diagnosis of the conservation state based on the multilayer point cloud results**

511 The present experimental campaign carried out on the Master Gate of San Francisco corroborates
512 the strong presence of pathological processes that are promoting the loss of material on
513 ornamental pieces and masonry blocks.

514 On the façades, it is possible to observe the presence of biological activity, mainly nitrophilic
515 lichens, and moisture (which generates black deposits on the masonry blocks) colonizing
516 approximately 4.14% and 14.17%, respectively, of the total surface (Fig. 14). Regarding the
517 biological colonization, façade B shows higher activity (5.96% in contrast with the 2.32% of
518 façade A), especially on the cornice, probably due to its situation (in an open space) and
519 orientation (south). However, façade A shows a large area affected by moisture (15.82%), in part
520 promoted by its orientation.

521 With respect to the deformations, façade A shows out-of-plane deformations (with a maximum
522 displacement of 0.18 m) on the lateral retaining walls (Fig. 17b). Those two walls are completely
523 split for the gate building by a construction joint (Fig. 23). On the left side, the maximum
524 deformations are close to 0.18 m but with a random distribution without showing the tilt of the
525 wall. This deformation could be due to a construction defect. On the other side, the maximum
526 deformation appears on the top of the wall, indicating a local tilt on the wall or a bubble in the
527 wall. The maximum value is also close to 0.18 m (Fig. 17b). Concerning Façade B (Fig. 17a), it
528 is possible to observe out-of-plane deformations on the vertical plane of the façade. No tilting
529 configuration is visible, since the deviations are almost constant with a maximum of 0.13 m. The
530 deviations are most probably due to construction defects or derived from the intensive
531 reconstruction carried out during 1986 (Fig. 9a).



532

533 **Figure 23:** Construction defects observed on façade A: (a) on the left side; and (b) on the right side.

534

535 Concerning the roof, a large discrepancy with respect to the hypothetical original roof can be
536 observed, with a maximum value of 0.21 m (Fig. 18). This disparity increases in the centre of the
537 construction system (the part with less thickness) suggesting an accommodation of the infill and
538 corroborating the significance of the reconstruction carried out during 1960 and 1986 (Fig. 9).
539 The greatest deviations are due to the significant permanent deformations that occurred around
540 the crack that is now apparently stabilized (Fig. 9b).

541 Finally, on the barrel vault, the high presence of salts and moistures (7.85% and 15.83% of the
542 total surface) have promoted the disaggregation of the masonry blocks, especially in the
543 intersection between the barrel vault and the façade B (Fig. 21), due to the atmospheric
544 contamination and the infiltrations of salts and water derived from the infill placed on it. Part of
545 these infiltrations, specifically 12.34% of them, are present on the most eroded parts of the barrel
546 vault (Fig. 22b).

547 In general, the analysis of the deformations does not show any significant problem with the
548 structure of the gate. Most of the deformations are construction defects promoted by the different
549 restorations of the Master Gate. Additionally, it is necessary to highlight that both façades show
550 large areas with black deposits and nitrophilic lichens affecting mainly the aesthetic of the
551 façades. These damages, can be remove by compatible cleaning strategies. It is also important to
552 fill the areas covered by lichens since these areas are more vulnerable to water infiltration and

553 chemical attacks. Concerning the state of conservation of the barrel vault, relevant damage
554 indicators (presence of white crusts, black deposits and disaggregation) are promoting important
555 material losses so this part of the gate requires urgent work such as roof waterproofing and joint
556 filling (with a compatible mortar) to avoid structural problems and further material losses.

557 **6 Conclusions**

558
559 At present, damage mapping in historical constructions requires a large user interaction to first
560 identify the damages presented on the monument and later to map them on 2D products such as
561 sections, plans or elevations. To solve these limitations, the present paper shows a methodology
562 based on the results captured by a TLS system (3D environment), that can combine radiometric
563 and geometric procedures with the aim of detecting a wide diversity of pathological processes
564 commonly presented on masonry construction.

565 On one hand, the radiometric analysis of the point clouds, by means of the TLS calibration as
566 well as the Fuzzy-k-means method, proves to be a potential solution to the detection of certain
567 types of pathological processes (such as biological colonization, salts or moisture), showing great
568 correlation with those pathological processes observed during the visual inspection.

569 On the other hand, geometrical strategies such as the PCA analysis, the RANSAC approach or
570 the CANUPO algorithm can work with geometrical features presented on the point cloud,
571 allowing the extraction of planes or areas with strong material losses.

572 The combination of both approaches offers new possibilities in the diagnosis of the conservation
573 state of our Cultural Heritage. By using this methodology, we demonstrated the ability not only
574 to evaluate the damage in a 3D environment but also the high correlation between visual indicators
575 of damages and results after analysing the multilayer point cloud.

576 Regarding the case study evaluated, the time invested to create the multilayer point cloud, in an
577 Intel® Core i5-3750K @ 3.40 GHz with 32 Gb of RAM memory, was approximately 14.75 hours:
578 (i) 5.5 hours to capture the structure (composed of 26 scan stations) and (ii) 9.25 hours to post-

579 process the data (6.0 hours of computer time and 3.25 hours of user time). The results obtained
580 for this field campaign corroborate the advanced state of degradation of the Master Gate. This
581 fact becomes more evident in the barrel vault, where there is a strong presence of salt crusts and
582 areas with high levels of moisture.

583 Considering the complexity of the diagnosis of the construction as well as the advantages and
584 limitations offered by the proposed method, future work will be focused on the following fields:
585 (i) radiometry; (ii) geometry; (ii) sensor integration; and (iv) visualization and management.

586 Regarding the radiometric aspect, further work will be focused on the integration of additional
587 sensors such as RGB or multispectral cameras, allowing a better separability between classes.

588 With respect to the geometrical features, further investigations will be focused on the design of
589 additional filters for the CANUPO algorithm, using the sharpness concept or the density of the
590 point cloud.

591 For sensor integration, data fusion of other non-destructive tests such as Ground Penetrating
592 Radar, boroscopic cameras or Scanning Electron Microscopes will be assessed to evaluate
593 possible internal defects present in the construction. The focus will be the creation of a
594 methodology for an accurate and complete diagnosis of the state of conservation of historical
595 masonry buildings, with the San Francisco Master Gate being one of the case studies. Finally,
596 such a large amount of data will be introduced into a multitemporal Geographical Information
597 System or Building Information Model to assist in the decision making.

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599
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